

■ Within each of the plots below:

Identify (theoretical) means and standard deviations of x , y .

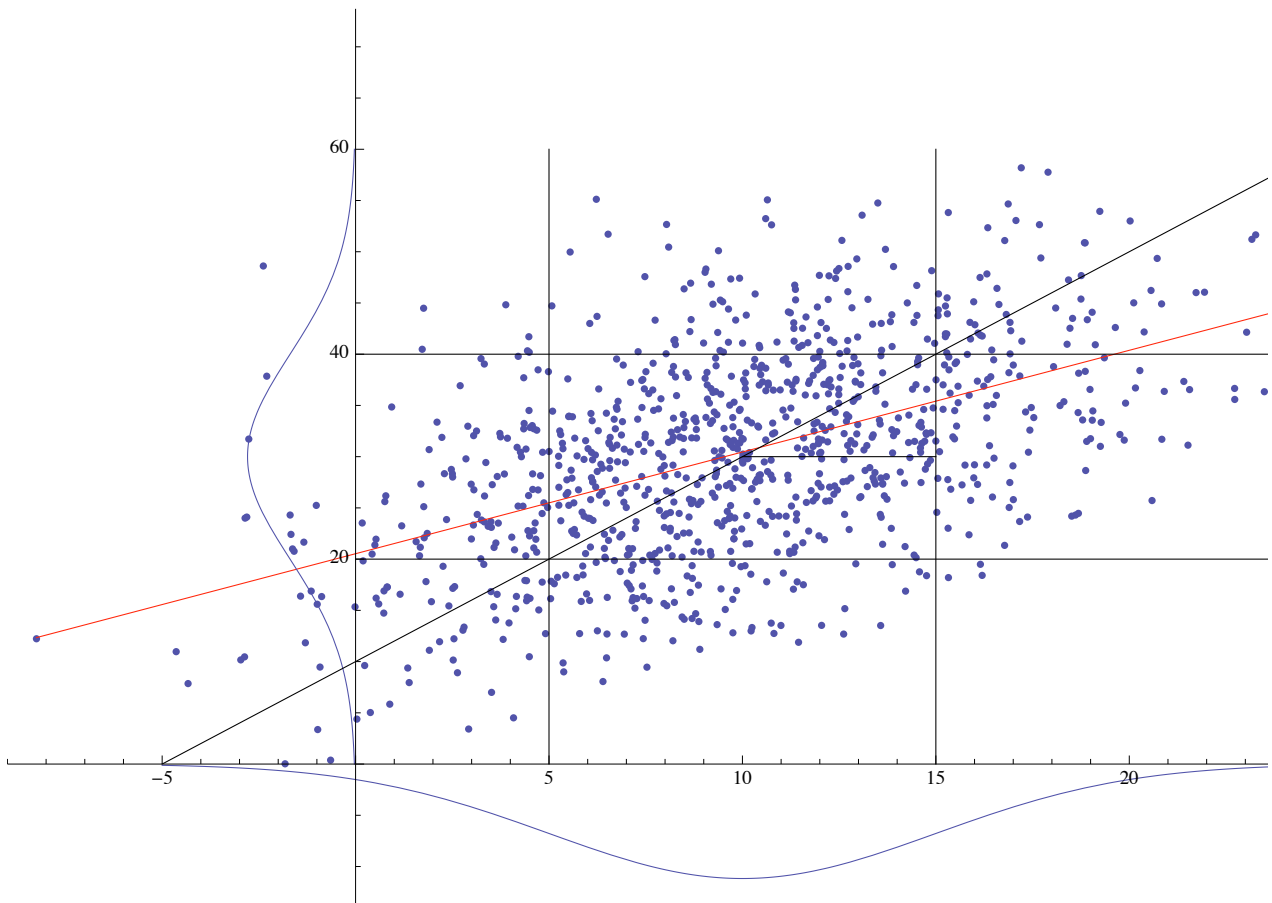
Identify the regression and naive lines.

Identify the correlation by noting the rise of the L. S. line relative to the naive line.

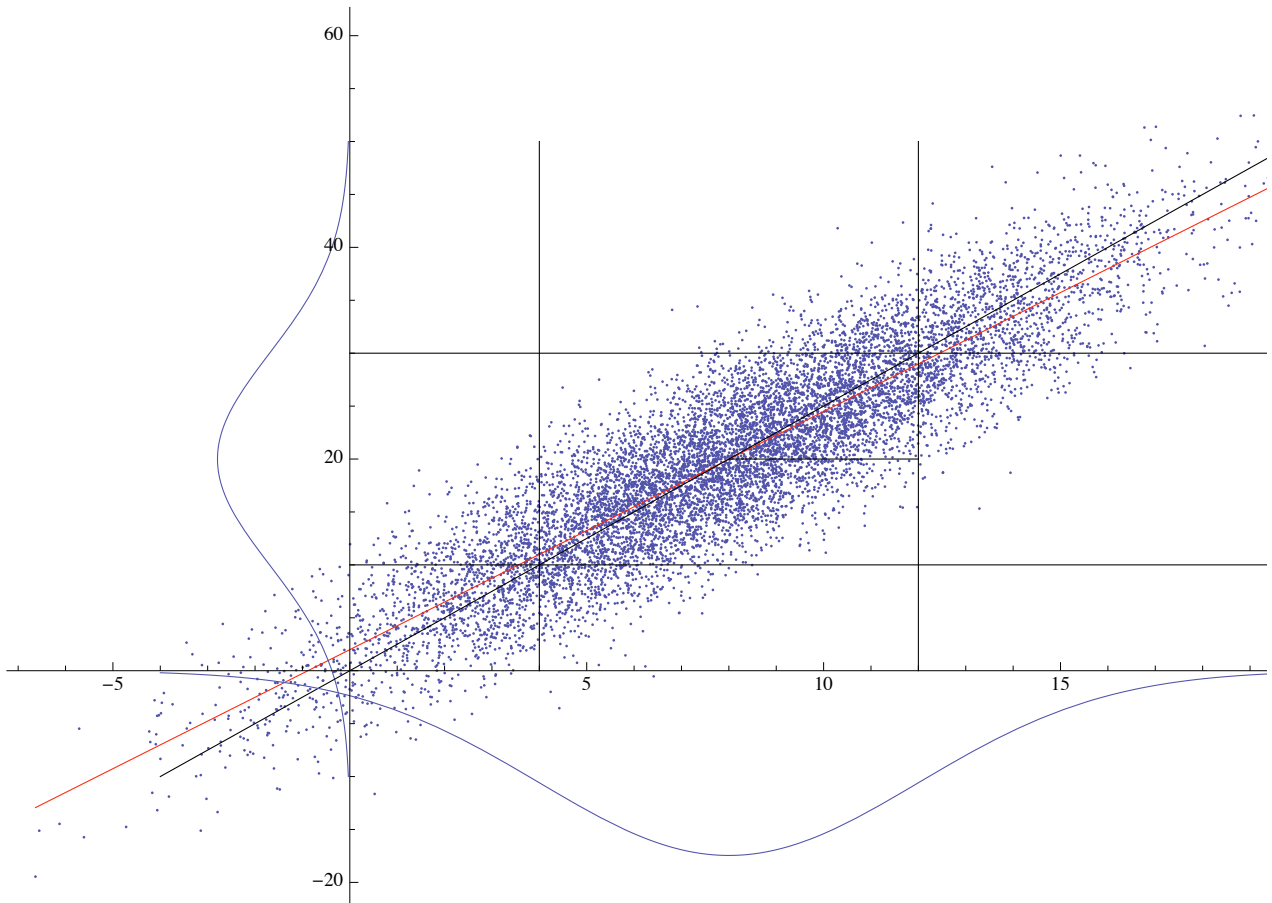
Identify the sd of y for (any) fixed x and see from the given specimen it is

$$\sqrt{1 - r^2} s_y.$$

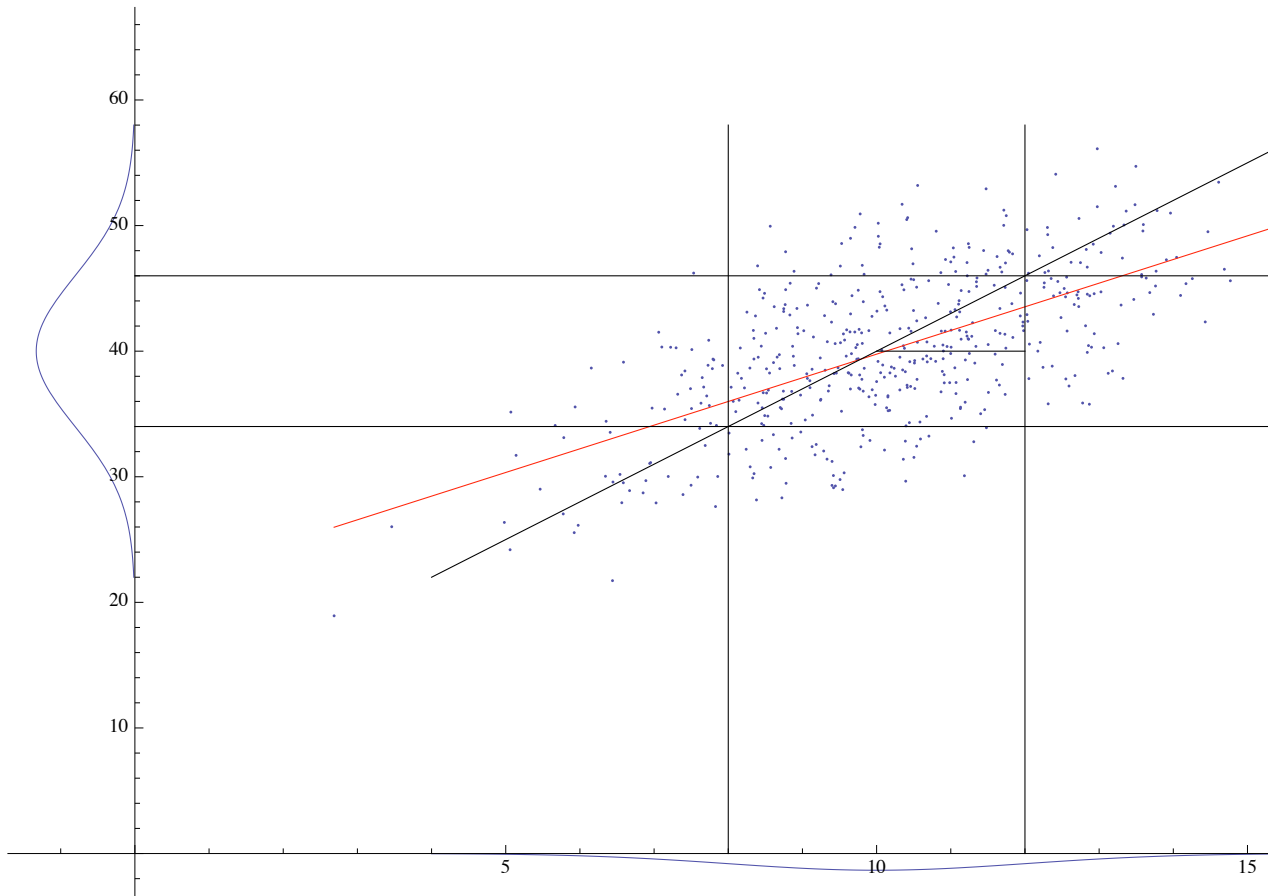
1. For this example the population means are 10, 30 the population sd are 5, 10. The correlation is 0.5.



2. Also, what is approximately the average y score for all of the points whose x is around 15?



3. Also, if $x = 14$ what are the mean and sd of the predicted value for y ?



4. A sample of 200 homes is selected at random from a large community, with equal-probability and (effectively) replacement. For each home in the population

x = 2005 valuation

y = 2010 valuation audit

It is known from the 2005 valuations that the x population mean is $\mu_x = 188,469$. Each of the 200 sample homes is audited to determine the 2010 valuation audit. From the sample we find

$$\bar{x} = 167,222$$

$$s_x = 74,873$$

$$\bar{y} = 241,770$$

$$s_y = 156,224$$

$$r = 0.78$$

a. Ignoring x altogether and just using y-scores, give the 95% z-based CI for μ_y .

b. Determine the regression based 95% CI for μ_y given by

$$\left(\bar{y} + (\mu_x - \bar{x}) r \frac{s_y}{s_x} \right) \pm 1.96 \sqrt{1 - r^2} \frac{s_y}{\sqrt{n}}$$

c. Compare the two CI (a), (b). How much wider is (a)? Notice that by exploiting regression in this way we've achieved a narrower 95% CI using the freely available x-scores associated with each sample home. Audits are by comparison very costly. So this beats using regular CI. We are required to know $\mu_x = 188,469$ however.

d. Is \bar{x} larger or smaller than the known μ_x ? If it is smaller then since this $r > 0$ that would suggest that we should increase our estimate of μ_y upwards from \bar{y} . Do you follow this reasoning? Is it happening here?

5. For problem 33 page 190

x = time, y = calories (averages at bottom)

| x | y | x ² | y ² | xy |
|-------|------|----------------|----------------|----------|
| 21.4 | 472 | 457.96 | 222 784 | 10 100.8 |
| 30.8 | 498 | 948.64 | 248 004 | 15 338.4 |
| 37.7 | 465 | 1421.29 | 216 225 | 17 530.5 |
| 33.5 | 456 | 1122.25 | 207 936 | 15 276. |
| 32.8 | 423 | 1075.84 | 178 929 | 13 874.4 |
| 39.5 | 437 | 1560.25 | 190 969 | 17 261.5 |
| 22.8 | 508 | 519.84 | 258 064 | 11 582.4 |
| 34.1 | 431 | 1162.81 | 185 761 | 14 697.1 |
| 33.9 | 479 | 1149.21 | 229 441 | 16 238.1 |
| 43.8 | 454 | 1918.44 | 206 116 | 19 885.2 |
| 42.4 | 450 | 1797.76 | 202 500 | 19 080. |
| 43.1 | 410 | 1857.61 | 168 100 | 17 671. |
| 29.2 | 504 | 852.64 | 254 016 | 14 716.8 |
| 31.3 | 437 | 979.69 | 190 969 | 13 678.1 |
| 28.6 | 489 | 817.96 | 239 121 | 13 985.4 |
| 32.9 | 436 | 1082.41 | 190 096 | 14 344.4 |
| 30.6 | 480 | 936.36 | 230 400 | 14 688. |
| 35.1 | 439 | 1232.01 | 192 721 | 15 408.9 |
| 33. | 444 | 1089. | 197 136 | 14 652. |
| 43.7 | 408 | 1909.69 | 166 464 | 17 829.6 |
| — | — | — | — | — |
| 34.01 | 456. | 1194.58 | 208 788. | 15 391.9 |

Let us suppose the data come from a random sample and the known population mean of time is 29 minutes.

a. Give the usual z-based 95% CI for the population mean of y ignoring x altogether.

b. Give the 95% z-based regression-based CI for the population mean of y .

c. How much narrower is (b) than (a)? Note: the sample size is rather small for the normal approximation to be confidently applied so regard this as a formal exercise of skills.